

Using thermal boundary conditions to engineer the quantum state of a bulk magnet

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Edited by Laura H. Greene, University of Illinois at Urbana–Champaign, Urbana, IL, and approved February 3, 2014 (received for review August 26, 2013)

The degree of contact between a system and the external environment can alter dramatically its proclivity to quantum mechanical modes of relaxation. We show that controlling the thermal coupling of cubic-centimeter-sized crystals of the Ising magnet $\text{LiHo}_x\text{Y}_{1-x}\text{F}_4$ to a heat bath can be used to tune the system between a glassy state dominated by thermal excitations over energy barriers and a state with the hallmarks of a quantum spin liquid. Application of a magnetic field transverse to the Ising axis introduces both random magnetic fields and quantum fluctuations, which can retard and speed the annealing process, respectively, thereby providing a mechanism for continuous tuning between the destination states. The nonlinear response of the system explicitly demonstrates quantum interference between internal and external relaxation pathways.

quantum magnetism | random fields | quantum annealing |
 quantum information | adiabatic quantum computing

The coupling of a sample to its environment is both a fundamental theoretical concept and a powerful experimental tool in classical thermodynamics. For quantum systems, contact between the internal degrees of freedom and the external world, often referred to as the “bath,” can change the measured outcome completely. Typically, such experiments involve a small number of particles sensitive to subtle changes in the external incoherent environment, such as ultracold atoms confined in precisely controlled optical potentials (1–3). With the search for viable solid-state qubits for quantum computing, the control of bath-induced decoherence in solids also has become an important topic for engineers and condensed-matter physicists. Approaches have centered on the nuclear spin bath (4–6), modifying it either with isotopic substitution (7) or radio frequency pulses (8), and on electrical control of the exchange interaction between electron spins in coupled quantum dots (9). The question of the importance of coupling to an external bath, as provided by a cryostat, has not been researched as intensively. Here, we show that by engineering the thermal boundary conditions for a macroscopic magnetic crystal, it is possible to select distinct low temperature states. Conditions of constant energy, as opposed to constant temperature, yield relatively fewer low energy contributions to the fluctuation spectrum and decouple the spin excitations responsible for that spectrum into separate oscillators. The experiments show the importance of thermal heat sinking for quantum annealing, also referred to as adiabatic quantum computation (10–13), as well as new protocols for generating quantum cluster states (14).

The $\text{LiHo}_x\text{Y}_{1-x}\text{F}_4$ family of insulating magnetic salts provides a physical manifestation of the simplest quantum mechanical spin model, the Ising model in transverse field (15). Pure LiHoF_4 (16, 17) is a ferromagnet with Curie temperature, $T_C = 1.53$ K. External magnetic fields can produce the longitudinal and transverse fields in the model, chemical substitution of Ho^{3+} ions by the nonmagnetic species Y^{3+} provides quenched disorder, and the anisotropy of the dipolar coupling produces random internal transverse fields (18–21) as well as competing ferromagnetic and antiferromagnetic interactions. The

combination of site dilution and external fields yields a wide variety of collective magnetic states, ranging from random field ferromagnet at $x = 0.44$ (22) to quantum spin glass at $x = 0.167$ (23). We focus here on the dilute limit of $x = 0.045$, for which there have been seemingly contradictory findings concerning the ground state.

The primary diagnostic of the ground state has been the AC magnetic susceptibility, whose imaginary part $\chi''(f)$ is the quotient of the long-wavelength magnetic fluctuation spectrum, $S(f)$, and the Bose factor, $(n(hf) + 1) = 1/(1 - \exp(-hf/kT))$, where h and k are Planck's and Boltzmann's constants, respectively. For our experiments, $hf \ll kT$ and hence $\chi''(f) = hf/kT S(f)$. The frequency at which the imaginary part peaks indicates the characteristic relaxation rate of the system, which for spin dynamics dominated by thermal activation over energy barriers will vary in accord with the Arrhenius law, $f = f_0 \exp(-E_A/kT)$ (15, 24, 25), precisely what we see for temperatures $0.15 \text{ K} < T < 1 \text{ K}$. Below $T \sim 0.15 \text{ K}$, deviations from Arrhenius behavior emerge (15, 24, 25); however, the nature of the deviations and their interpretation has been contested (26). One class of experiments found a low-frequency narrowing of the spectrum with decreasing T (24, 27, 28), accompanied by the magnetic equivalent of optical hole burning in the nonlinear response, where effectively isolated, mesoscopic clusters of spins can be addressed and manipulated using a pump/probe technique (24). A magnetic field applied transverse to the Ising axis introduces quantum fluctuations, and can influence the relaxation pathways of the coherent clusters (28). Moreover, muon spin-relaxation (μSR) studies have shown that the persistent spin-fluctuation rate remains constant down to $T = 0.02 \text{ K}$, consistent with a spin-liquid ground state (29). By contrast, a second class of magnetic susceptibility studies found that $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ behaved as a paramagnet approaching a spin-glass transition, which extrapolation suggests to occur at $T_g \sim 0.04 \text{ K}$, with a magnetic fluctuation spectrum that broadened symmetrically as

Significance

The interactions of a material with its environment can determine its behavior and induce changes of state. We show that, at temperatures near absolute zero, a magnetic material can be made more quantum mechanical by isolating it from the environment. Local clusters of spins within the material stay liquid and refuse to freeze. An oscillating magnetic field serves as an effective tool to address and manipulate these “protected” spin clusters, while a DC magnetic field can enhance the spin-tunneling rate and lead to quantum speedup. When the material is more strongly connected to a heat bath, the local magnetic clusters behave more classically and freeze en masse into a glassy state.

Author contributions: M.A.S., D.M.S., G.A., and T.F.R. designed research; M.A.S. and D.M.S. performed research; M.A.S., D.M.S., and T.F.R. analyzed data; and M.A.S., D.M.S., G.A., and T.F.R. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

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the temperature was lowered (25). In this picture, the characteristic dissipative response moves more quickly to low frequency as the system as a whole freezes.

The most significant distinction between the two classes of susceptibility experiments is the heat sinking of the sample to the cryostat. For the measurements yielding a spin liquid, a single crystal measuring ($5 \times 5 \times 10$) mm³ was heat sunk by sapphire rods pressed against the sample on either end of the long axis (24); in the spin-glass case a ($0.57 \times 0.77 \times 7.7$) mm³ sample was glued to a sapphire rod running along its length (25). The sapphire rods are then thermally anchored to the mixing chamber of the dilution refrigerator, coupling them to the environmental heat bath. If the thermal boundary conditions of the sample change appreciably, then the internal state of the system also may be expected to change. Just as the application of a transverse magnetic field affects the spin cluster dynamics and their coupling to the external world in this system (28), thermal boundary conditions can enhance or destroy isolated spin degrees of freedom, tune the system between classical and quantum mechanical limits (30), and alter the relative energies of competing ground states.

Results and Discussion

To test whether such tuning can be realized experimentally, we measured the linear and nonlinear AC magnetic susceptibility of the same $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ crystal studied in ref. 24, but now in two different thermodynamic limits (Fig. 1A). For the first configuration (Fig. 1A, *Left*), the sapphire heat-sinking rods are in direct, spring-loaded contact with the sample on each end, and are mechanically connected (in vacuo) to the cryostat cold finger on the other. In this “strongly coupled” geometry, the ends of the sample define lattice isotherms. In the second configuration, the sapphire rods are mechanically separated from the sample with a 4-mm average vacuum gap by using Teflon spacers at the rear of the sapphire rods (Fig. 1A, *Right*). In this “weakly coupled” geometry, the dominant thermal link between the sample and the cryostat is through the Hysol (epoxy resin) body of the susceptometer coil form. The thermal conductivity of the sapphire at $T = 0.1$ K allows an energy flow of ~ 10 nW/mK between the sample and cryostat, to be compared with that of the disconnected geometry’s 0.3 nW/mK, and blackbody heat flow from the vacuum can at $T = 4.2$ K of 1×10^{-8} nW/mK, much less than the heat flow through the Hysol coil form in the weakly coupled geometry. The

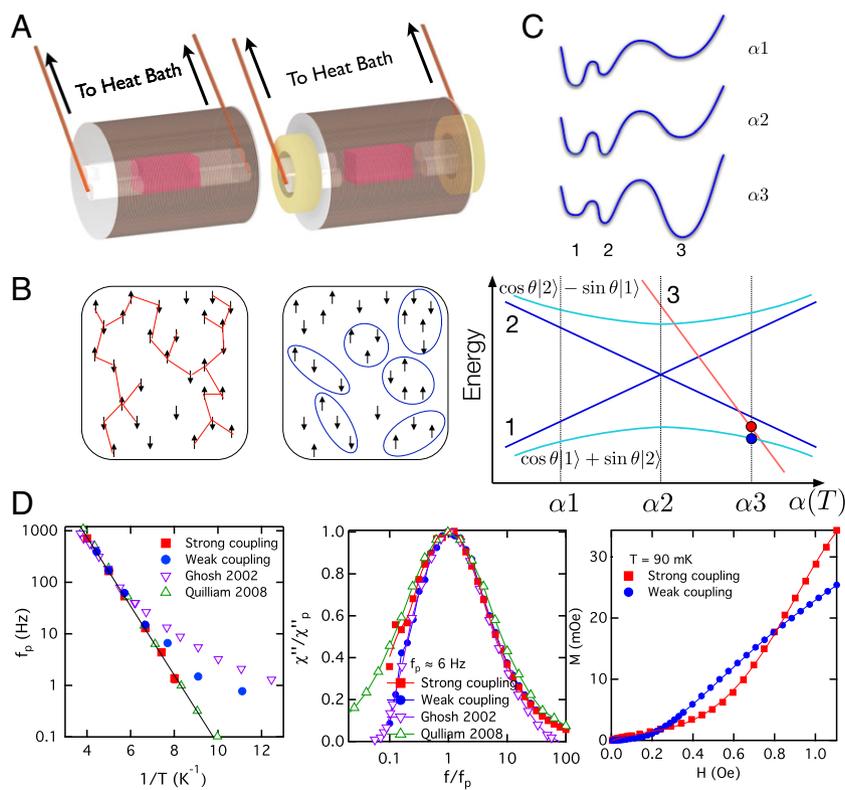


Fig. 1. Effects of thermal boundary conditions on $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$. (A) Schematic of experimental arrangement. The sample sits at the center of an AC susceptometer coil set. Sapphire rods connected via copper wires to the cryostat cold finger provide thermal contact to the sample. (*Left*) Rods in direct contact with sample; (*Right*) Teflon spacers at the backs of the rods impose a 4-mm vacuum gap between rods and sample, making the epoxy resin coil assembly the dominant route for thermalization. (B) Cartoon of spin configurations inside the $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ crystal for the two experimental configurations in A. (*Left*) In the presence of strong thermal coupling to a heat reservoir, the system forms a glassy network dominated by thermal fluctuations. (*Right*) In the absence of a strong connection to the reservoir, isolated spin clusters with discrete quantum transitions coupled weakly to the continuum of excitations of other clusters are an important feature of the low temperature response. (C) At *Top* is a schematic showing the thermal evolution (associated with the mean field from other clusters) of the potential energy for different states of a typical spin cluster as shown in B. *Bottom* frame shows how quantum mixing of states alters the outcome of the cooling process, with a quantum mixture of eigenstates 1 and 2 rather than the lowest energy state 3 emerging for cooling rapid compared to decoherence rates. (D) Measured effects of changing thermal coupling conditions. (*Left*) Peak frequency of imaginary susceptibility as a function of inverse temperature for the two configurations drawn in A, compared with values published in refs. 24 and 25. (*Center*) Lineshapes of the imaginary susceptibility under different thermal conditions for the same peak frequency. Measurements in the weakly coupled thermal configuration show low-frequency spectral narrowing not observed in the connected configuration. (*Right*) Magnetization curves at fixed frequency for the two thermal configurations, showing markedly different functional forms and field scales for the onsets of non-linearity and saturation.

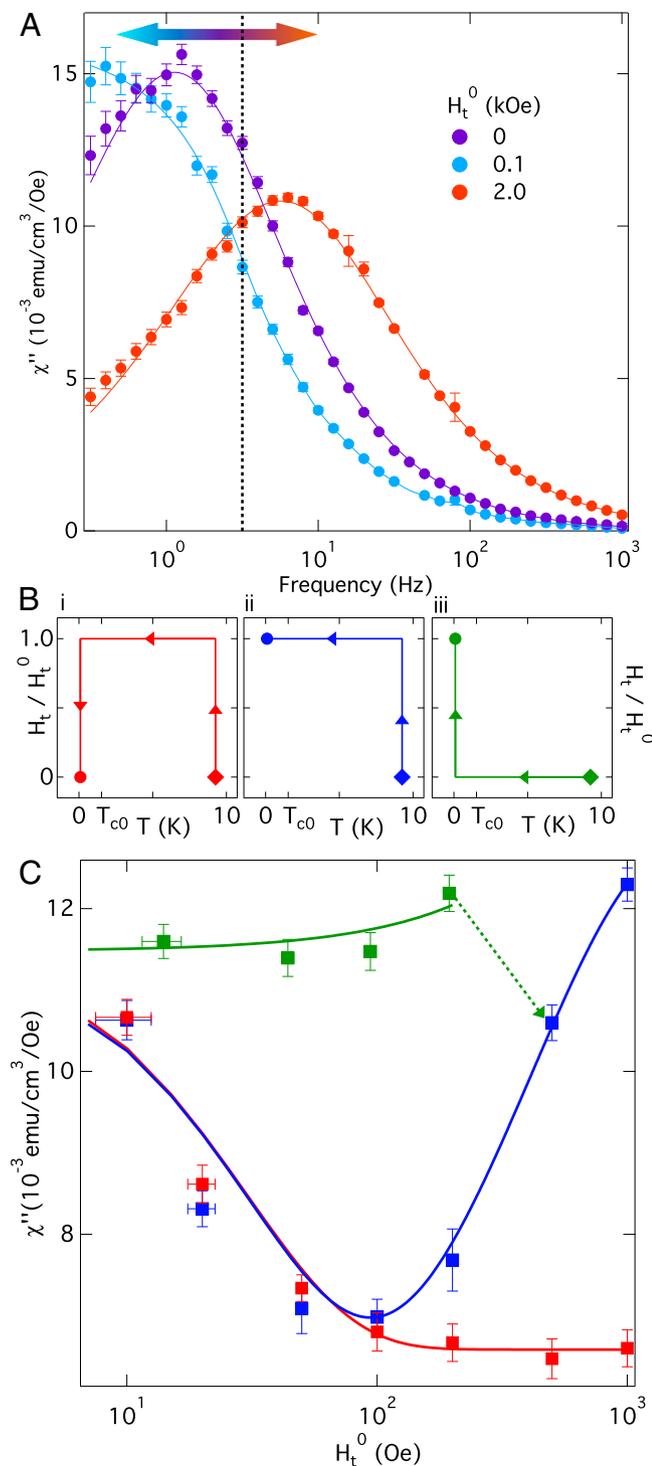


Fig. 3. Random-field pinning and quantum speedup with transverse field. (A) Imaginary susceptibility of $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ with weak coupling to the bath after cooling from 9 to 0.09 K in a transverse field H_t^0 . The spectrum moves nonmonotonically with H_t^0 , first slowing from enhanced random field pinning and then moving to higher frequency via transverse field-induced tunneling. Dashed line at 3.1 Hz indicates constant-frequency cut used in C. (B) Trajectories through H_t - T space. (C) Constant-frequency response of the imaginary part of the susceptibility following the three different cooling trajectories over a range of transverse fields. In the quantum annealing trajectory (i), as in ii, where the quantum fluctuation rate remains constant approaching the final state, $H_t^0 \sim 0.1$ kOe demarcates different response regimes. The classical annealing trajectory (iii) shows a weak quantum speedup at low fields followed by an instability at fields above 0.5 kOe that yields a tunneling transition to branch (ii) with a timescale ~ 1 d.

depending on whether the cooling rate is faster than the decoherence rate produced by the environment not incorporated in the Hamiltonian including the mixing terms. These decoherence times are fixed by the rate at which phonons can be supplied to the bath, which is in turn controlled by the heat sinking.

Another diagnostic of the magnetic state is the probe amplitude-dependent response, where we observe how the system departs from the linear, small signal regime. The right-hand side of Fig. 1D demonstrates a profound difference between the nonlinear susceptibilities for the two couplings: for the adiabatic limit, we observe an s-like Brillouin term superposed on a linear background, and for strong coupling to the bath, the linear regime persists to higher drive field, after which the response grows more dramatically to cross that for weak coupling to the bath.

Previous work has shown that transverse fields H_t applied to $\text{LiHo}_x\text{Y}_{1-x}\text{F}_4$ induce both quantum fluctuations and static random fields. Given that the random field amplitudes and quantum tunneling rates scale as H_t and H_t^2 , respectively (21, 22), random field effects, including pinning and associated slowdown of spin fluctuations, should dominate at small H_t . As H_t is increased beyond the crossover field where tunneling rates and pinning energies are in balance, quantum speedup should become visible. A crossover between regimes dominated by H_t -induced longitudinal random fields and H_t -induced tunneling was in fact observed in the more concentrated random ferromagnet, $\text{LiHo}_{0.44}\text{Y}_{0.56}\text{F}_4$ (22, 39). For weak coupling, Fig. 3A displays precisely the anticipated effects even in the $x = 0.045$ sample, namely a softening of the spectrum as we raise H_t from 0 to 100 Oe, and then a hardening upon further increasing H_t to 2,000 Oe. Consistent with classical pinning, the initial softening effect is visible only when cooling in field from high temperature, whereas the high transverse field (2 kOe) hardening is history-independent and therefore consistent with H_t -induced quantum speedup.

Fig. 3 B and C, showing the behavior of the spin liquid after preparation via different trajectories through H_t - T space, supports the random field-quantum crossover description for weak heat sinking. In addition to the quantum annealing protocol (i), we also followed the mixed H_t /thermal schedules (ii) where the transverse field H_t^0 is applied before cooling, but not removed at lowest T as in (i), and (iii) where the transverse field is only applied after cooling to the lowest T . Despite the data being collected at identical (T, H_t^0) , the spectra do not coincide below $H_t^0 \sim 500$ Oe. The classical pathway (iii) becomes unstable over the course of a day for $H_t^0 \sim 500$ Oe, and the two protocols merge over repeated measurements of the spectrum. Above this field scale, the transverse field is large enough to produce the quantum fluctuations required to overcome pinning of spin configurations in the search for equilibrium. For even larger transverse fields ($H_t > 3.5$ kOe), the physics of quantum-level crossings for single ions and pairs of ions, determined both by purely electronic and nuclear hyperfine interactions, emerges and can be probed directly (28, 40).

An important result is that tuning the system state with H_t^0 requires thermal cycling above $T = 9$ K before changing the transverse field. Warming above the Curie temperature of the pure compound, $T_C = 1.53$ K, or even to $T = 4$ K, is not sufficient to reset the system upon cooling. Rather, the low temperature state only responds to a change in H_t^0 if the spins are thermally excited above the 9.4 K splitting between the Ising ground-state doublet and the first excited-state singlet (15). This points once again to the fundamental quantum nature of the ground state when isolated from the incoherent thermal bath.

We explore in Fig. 4 the spectral characteristics of the weakly coupled spins after quantum annealing, probing both the linear and nonlinear response. There appear to be a continuous set of low-temperature states that the system can access depending on the strength of the cooling field. For $H_t^0 < 0.1$ kOe, we see that χ'' behaves as in Fig. 3A, where the cooling field was maintained to

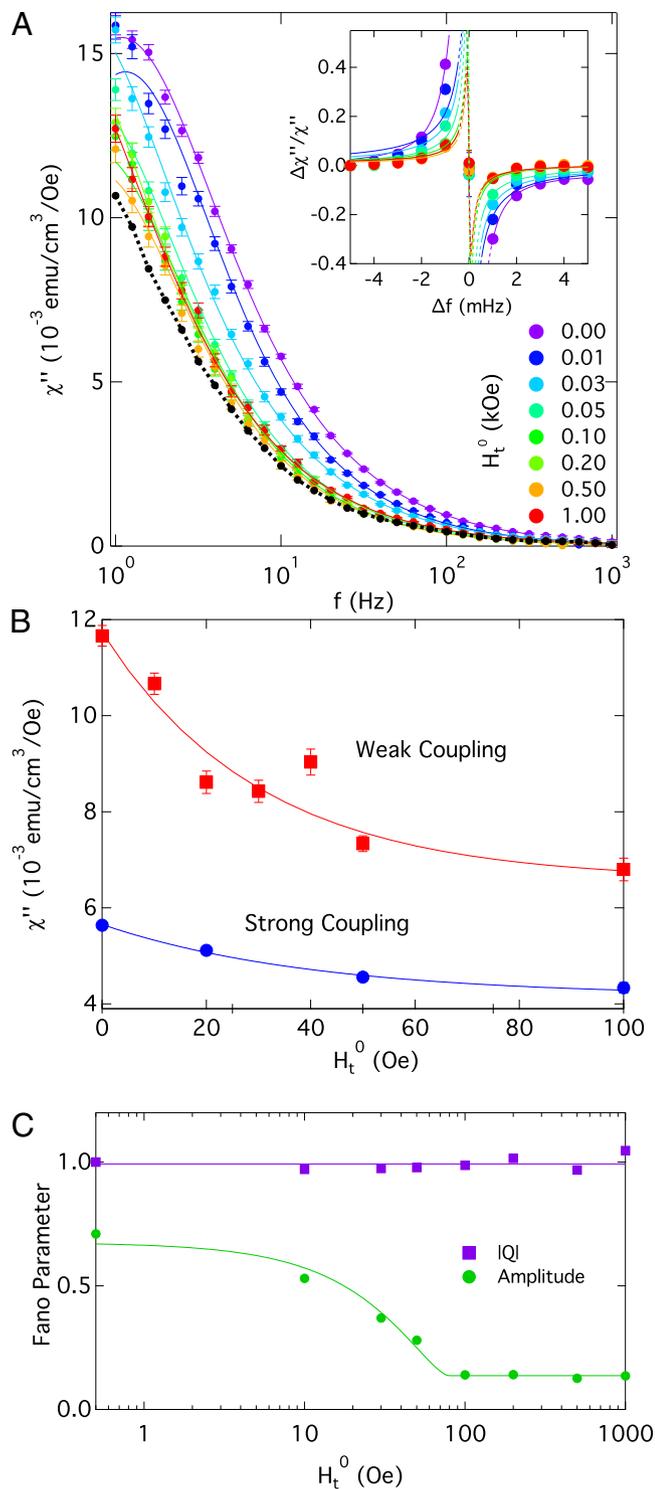


Fig. 4. Spectral character of the linear and nonlinear response. **A** Imaginary part of the susceptibility from 1 Hz to 1 kHz after quantum annealing in a series of transverse fields with the crystal weakly coupled to the bath. The curve in black is the dissipative response of the sample in the strongly coupled limit with $H_t^0 = 0$. An in situ GaAs Hall magnetometer was used to directly measure the applied transverse field. (*Inset*) Nonlinear pump-probe spectroscopy for the same quantum annealing trajectories as in the main panel, with a 19.95 Hz/0.3 Oe pump field. The Fano resonance fits (smooth curves, Eq. 1) indicates interference between excitations of discrete spin cluster states and those in the bath; dashed lines show predicted behavior for the resonances for Δf less than the experimental resolution. **(B)** Constant-frequency ($f = 3.1$ Hz) cuts of the imaginary susceptibility as a function of the

achieve the final state. In particular, there is a softening with increasing transverse field, corresponding to the random fields present on the cool-down that pin the spin configuration even after the transverse field is shut off at low T . On the other hand, the final state is much less dependent on $H_t^0 > 0.1$ kOe, consistent with the capability of quantum annealing to produce approximately the same final state independent of the transverse field during cooling; the discrepancies found at low frequencies may be linked to small differences in precisely how the random field regime for $H_t < 0.1$ kOe was traversed.

We have shown that for weak thermal coupling, $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ approaches a different quasi-equilibrium state than for strong thermal coupling. In particular, the former state seems to display more apparently quantum mechanical traits, most notably a spectrum with a higher characteristic frequency than predicted from thermal activation, a nearly dissipationless response at low frequencies, and more acute sensitivity to externally applied transverse fields (Fig. 4B). As in optical spectroscopy, pump/probe studies of $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$ can be used to determine the extent to which the response spectrum is due to an inhomogeneous mixture of different oscillators with different resonance frequencies or to relaxation of coupled degrees of freedom. For strong thermal coupling, we simply observe the earmarks of heating when applying a large (~ 0.3 Oe) pump field. By contrast, for weak thermal coupling we observe a Fano resonance centered at the pump frequency (Fig. 4A, *Inset*), corresponding to a discrete oscillator coupled to a continuum:

$$\Delta\chi'' \propto \frac{\left(\frac{Q\Gamma}{2} + \Delta f\right)^2}{\Delta f^2 + \left(\frac{\Gamma}{2}\right)^2}, \quad [1]$$

where Δf is the distance from the center point of the resonance, Γ is the characteristic width of the resonance and the Fano parameter Q parameterizes the asymmetry of the resonance. The Fano effect is a quantum interference effect, first described to explain the absorption spectra of gas molecules (41) and later observed in a wide variety of quantum two-level systems ranging from semiconductor quantum wells (42) to the Bose-Einstein Condensation to Bardeen-Cooper-Schreiffer crossover in cold atom experiments (43, 44). In $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$, the presence of this resonance for a weakly linked thermal bath, and absence for a strongly linked bath, again confirm the need for a quantum mechanical description of the ground and low-lying excited states for weak linkage to the bath. We plot in Fig. 4C the results of fits of Eq. 1 to our data. They reveal that although the coupling constant Q is essentially independent of the transverse field applied while cooling, the amplitude of the resulting Fano resonance, and hence the number of oscillators coupled to the bath, can be tuned continuously by H_t^0 . The latter undergoes a type of phase transition at a critical $H_{tc}^0 \sim 0.1$ kOe identified in the linear response experiments. It varies as $C + (H_{tc}^0 - H_t^0)^\alpha$ below 0.1 kOe with $\alpha = 1.5 \pm 0.1$, and matches the constant C in remarkable field-independent fashion above 0.1 kOe. This means that some local oscillators, most likely associated with the motion of spins near pinning sites, survive the larger quantum fluctuations brought about by the larger transverse field.

Our results have both fundamental and practical implications. On the fundamental side, they mean that even for macroscopic

cooling field for the two couplings to the bath. **(C)** The Fano coupling parameter Q (Eq. 1) is essentially independent of cooling field, but the amplitude of the resonance, and hence the number of discrete oscillators coupled to the bath, decreases until the demarcation field $H_{tc}^0 \sim 0.1$ kOe identified in Fig. 3C, and then stabilizes at a finite value.

solid-state systems, thermal coupling has effects similar to those of stopping gases that destroy quantum effects in atomic physics experiments via collisions. Weakening the thermal coupling converts a classical glass into a stable system with the earmarks of a quantum spin liquid. The practical implication is that the performance of quantum annealing machines (10), of which our apparatus is one example (used here to solve the specific problem of finding

the most probable spin states for a crystal of $\text{LiHo}_{0.045}\text{Y}_{0.955}\text{F}_4$), can depend strongly on the coupling to their heat baths.

ACKNOWLEDGMENTS. G.A. is grateful to N. Chancellor for discussions. The work at The University of Chicago was supported by Department of Energy Basic Energy Sciences Grant DE-FG02-99ER45789 and in London via the COMPASS programme grant funded by the UK Engineering and Physical Sciences Research Council.

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